

1. Find $\lim_{(x,y) \rightarrow (0,0)} \frac{4xy^2}{x^2+y^2}$, if it exists.
2. Find the Largest and the smallest value of $f(x, y) = 2xy$ on the ellipse $x^2/16+y^2/4 = 1$.
3. Suppose that f and g are scalar functions with continuous first and second order partial derivatives throughout a region D that is bounded by a closed piecewise smooth surface ∂D .

(a) Show that

$$\iint_{\partial D} f \nabla g \cdot \mathbf{n} d\sigma = \iiint_D (f \nabla^2 g + \nabla f \cdot \nabla g) dV$$

(b) show that

$$\iint_{\partial D} (f \nabla g - g \nabla f) \cdot \mathbf{n} d\sigma = \iiint_D (f \nabla^2 g - g \nabla^2 f) dV$$